

**ARULMIGU PALANIANDAVAR ARTS COLLEGE FOR WOMEN,
PALANI**

DEPARTMENT OF MATHEMATICS

Learning Resources

Title of the paper: REAL ANALYSIS

Prepared By

Dr.K.Meena, Associate Professor and Head

ONE MARK QUESTIONS WITH ANSWERS

REAL ANALYSIS

- Two sets A and B are equivalent if There exists a -----from A to B
a) injection b) bijection c) surjection d) homomorphism. Ans: b) bijection
- Let $N = \{1, 2, 3, \dots, n, \dots\}$ and $E = \{2, 4, \dots, 2n, \dots\}$
The correct statement is ----- a) N and E are equivalent sets
b) N and E are equal s c) N and E are infinite sets d) N and E are finite sets
Ans: a) N and E are equivalent sets
- The incorrect statement from the following statement is -----
a) $E = \{2, 4, \dots, 2n, \dots\}$ is a countable set b) Z is a countable set c) N is a countable set d) R is a countable set
Ans: d) R is a countable set
- The incorrect statement from the following statement is -----
a) $N \times N$ is a countable set b) Q is a countable set c) N is a countable set d) R is a countable set
Ans: d) R is a countable set
- The incorrect statement from the following statement is -----
a) $(0, 1]$ is uncountable b) $[0, 1]$ is uncountable c) Q is uncountable
d) $\{0\} \cup \{1\} \cup \{2\}$ is uncountable
Ans: d) $\{0\} \cup \{1\} \cup \{2\}$ is uncountable
- The set $\{2, 4, \dots, 2n, \dots\}$ is ----- a) countable b) uncountable c) finite d) none
Ans: a) countable

Say True or False

- Every finite set can be equivalent to a proper subset of itself Ans: False
- Every infinite set can be equivalent to a proper subset of itself Ans: True
- A set A is said to be countably infinite if A is ----- to the natural number N
Ans: equivalent

10. A is said to be countable if it is ----- Ans: finite or countably infinite
11. The countable set is -----a) $[0,1]$ b) \mathbb{R} c) \mathbb{Q} d) \mathbb{C} Ans: c) \mathbb{Q}
12. \mathbb{Q} is ----- in \mathbb{R}
 a) open b) closed c) not open d) uncountable Ans: c) not open
13. In any metric space (M,d) the diameter of the empty set Φ is -----
 a) 0 b) 1 c) ∞ d) $-\infty$ Ans: $-\infty$
14. In a metric space (M,d) Let $A \subseteq M$. The diameter of A denoted as $d(A)$ is defined as ----
 a) $\text{g.l.b } \{d(x,y)/x,y \in A\}$ b) $\text{l.u.b } \{d(x,y)/x,y \in A\}$
 c) $\text{g.l.b } \{d(x,y)/x \in A, y \in A\}$ d) $\text{l.u.b } \{d(x,y)/x,y \in A\}$
 Ans: b) $\text{l.u.b } \{d(x,y)/x,y \in A\}$
15. The diameter of any non empty subset in a discrete metric space is -----
 a) 0 b) ∞ c) $-\infty$ d) 1 Ans: d) 1
16. In a discrete metric space M the diameter of $A = \{1,5,7,9\}$ is-----
 a) 0 b) 1 c) 9 d) 8 Ans: d) 8
17. In (\mathbb{R},d) The diameter of $[0,1] \cap [2,3] =$ -----
 a) 0 b) $-\infty$ c) 4 d) 3 Ans: b) $-\infty$
18. In \mathbb{R} with usual metric for $a \in \mathbb{R}$ open ball $B(a,r) =$ -----
 a) $(a-r, a+r)$ b) $[a-r, a+r]$ c) $(a-r, a+r]$ d) $[a-r, a+r)$ Ans: a) $(a-r, a+r)$
19. In $[0,1]$ with usual metric for open ball $B(0,1/4) =$ -----
 a) $(-1/4, 1/4)$ b) $[0, 1/4)$ c) $(-1/4, 0)$ d) $(0, 1/4)$ Ans: b) $[0, 1/4)$
20. If M is In a discrete metric space Then $B(a,2) =$ -----
 a) $\{0\}$ b) M c) Φ d) 2 Ans: b) M
21. In \mathbb{R} with usual metric $[a,b]$ is -----
 a) Closed b) open c) either closed or open d) neither closed nor open
 Ans: d) neither closed nor open
22. In \mathbb{R} with usual metric every singleton set is -----Ans: closed
23. In \mathbb{R} with usual metric every closed ball is a -----Ans: closed set
24. The set of irrational numbers in \mathbb{R} is -----
 a) Closed b) open c) complete d) dense Ans: d) dense
25. The set of all limit point s of A is called the -----of A .
 Ans: derived set
26. If $A = \{0, 1, 1/2, 1/3, \dots, 1/n, \dots\}$ then the derived set of A denoted by $D(A)$ is ----- a) 1 b) $\{0\}$ c) A d) $\{0,1\}$ Ans: b) $\{0\}$
27. A subset A of a metric space M is said to be -----in M if $A = M$.

Ans: dense

28. A metric space M is said to be separable if ----- Ans: there exists a countable dense subset in M .

Say True or False

29. A set is closed iff it contains all its limit points – Ans: True

30. A set A is closed iff $A = \bar{A}$ Ans: True

31. In \mathbb{R} with usual metric \mathbb{Q} is dense Ans: True

32. \mathbb{R} with discrete metric is separable Ans: False

33. In a discrete metric space no proper subset is dense Ans: True

34. A metric space M is said to be complete if every Cauchy sequence in M ----- Ans: converges to a point in M

35. The metric space $(0,1]$ with usual metric is -----

a) complete b) not complete c) closed d) none Ans: b) not complete

36. A subset A of a complete metric space M is complete if A is -----

Ans: closed

37. State Baire's category theorem Ans: Any complete metric space is Second category

Say True or False

38. A subspace of a complete metric space is complete. Ans: False

39. Any metric space which is of second category is complete. Ans: False

40. Any discrete metric space is of second category. Ans: True

41. If f is continuous function from a metric space M_1 to a metric space M_2 then ----- a) A is open in $M_1 \implies f(A)$ is open in M_2

b) A is closed in $M_1 \implies f(A)$ is closed in M_2

c) A is open in $M_2 \implies f^{-1}(A)$ is open in M_1 d) If $A \subset M_1$,

then $f(A) = \bar{f(A)}$. Ans: c) A is open in $M_2 \implies f^{-1}(A)$ is open in M_1

42. Composition of two continuous function is ---- Ans: continuous

43. In usual metric there exists a continuous function from -----

a) $(0,1)$ onto $[0,1]$ b) $(0,1)$ onto \mathbb{R} c) $[0,1]$ onto $(0,1)$ d) $(0,1)$ onto \mathbb{Q}

Ans: b) $(0,1)$ onto \mathbb{R}

44. A function $f: M_1 \rightarrow M_2$ is said to be an ----- if $f(G)$ is open in M_2 for every set G in M_1 continuous. Ans: open map

45. \mathbb{R} with usual metric is not homeomorphic to \mathbb{R} with -----

Ans: discrete metric

46. A continuous function $f: M_1 \rightarrow M_2$ need not be ----- on M_1 .

Ans: uniformly continuous

47. A function whose domain is a discrete metric space is -----

Ans: continuous

48. If $f: M_1 \rightarrow M_2$ is a homeomorphism then f is continuous and an -----

Ans: open map

49. If $f: M_1 \rightarrow M_2$ is a homeomorphism then f and f^{-1} are -----

Ans: continuous

50. If $f: M_1 \rightarrow M_2$ is uniformly continuous on M_1 then f is -----

Ans: continuous at every point on M_1

51. If $f: M_1 \rightarrow M_2$ is a homeomorphism then f^{-1} is -----

Ans: homeomorphism.

52. Any isometry from one metric space to another is a -----

Ans: homeomorphism.

53. If $f: \mathbb{R} \rightarrow \mathbb{R}$ defined by $f(x) = x^2$ is continuous but not ----- on \mathbb{R} .

Ans: uniformly continuous.

Say True or False

54. If $f: \mathbb{R} \rightarrow \mathbb{R}$ defined by $f(x) = kx$, $x \in \mathbb{R}$ uniformly continuous

Ans: True

55. If $f: [0, 1] \rightarrow \mathbb{R}$ defined by $f(x) = x^3$ uniformly continuous.

Ans: True

56. Any open intervals in \mathbb{R} are homeomorphic. Ans: True

57. If $f: [0, 1] \rightarrow \mathbb{R}$ defined by $f(x) = x^2$ uniformly continuous $[0,1]$.

Ans: True

58. If $f: \mathbb{R} \rightarrow \mathbb{R}$ & $g: \mathbb{R} \rightarrow \mathbb{R}$ are uniformly continuous then fg uniformly continuous . Ans: False

59. Any homeomorphism from one metric space to another is a isometry.

Ans: False

60. If $f: M_1 \rightarrow M_2$ is a continuous bijection then $f^{-1}: M_2 \rightarrow M_1$ is also continuous. Ans: False

**61. Let $[1, 2] \cup [3,4]$ with usual metric Then M IS ----- a) connected
b) disconnected c) compact d) none Ans: b) disconnected**

**62. \mathbb{R} is ----- a) compact b) connected c) disconnected
d) none Ans: c) disconnected**

**63. Any discrete metric space M with more than one point is -----
a) compact b) connected**

c) disconnected d) none Ans: c) disconnected

64. M is connected iff every continuous function $f : M \rightarrow (0,1)$ is -----
Ans : not onto.

65. A subspace of \mathbb{R} is connected iff -----Ans: it is an interval

66. A subspace of a connected metric space -----a) connected b) need not be connected c) is finite d) is countable .

Ans : b) need not be connected

67. Let f be real valued continuous function defined on an interval I . Then f takes every value between any two values it assumes. This statement is known as ----- Ans: The intermediate value theorem.

68. If f is non-constant real valued continuous function on \mathbb{R} Then the range of f is -----Ans: uncountable

69. $A = \{ (x, y) / x^2 + y^2 = 1 \}$ is a ----- subset of \mathbb{R}^2 Ans: connected.

70. $[0, 1]$ is ----- subset of \mathbb{R} with discrete metric a) connected
b) compact c) not a connected d) none Ans: not a connected

71. If A and C are connected subset of metric space M and if $A \subseteq B \subseteq C$, Then B is ----- Ans: connected

72. Union of two connected sets -----Ans: need not be connected.

73. Which of the following is a connected subset of \mathbb{R} with usual metric ?
a) \mathbb{N} b) \mathbb{R} c) $(0, 1) \cup (1, 2)$ d) \mathbb{Z} Ans: b) \mathbb{R}

Say True or False

74. \mathbb{R} is connected. Ans: True

75. \mathbb{Q} is connected. Ans: False

76. A subspace of a connected subsets of a metric space M , then $A \cup B$ is connected. Ans: False

78. If A and B are connected subsets of M and $A \cap B \neq \Phi$ then $A \cup B$ is connected .Ans: True

79. If M is a metric space and $x \in M$ then $\{x\}$ is a connected subset of M .
Ans: True

80. Continuous image of a connected set is connected. Ans: True

81. Which of the following is a compact subset of \mathbb{R} with usual metric ?
a) \mathbb{N} b) \mathbb{R} c) $[0, 5]$ d) $\{1, 1/2, 1/3, \dots, 1/n, \dots\}$ Ans: c) $[0, 5]$

82. Which of the following is a compact metric space with usual metric ?
a) \mathbb{R} b) $(0, 1)$ c) $[0, \infty)$ d) $[0, 1]$ Ans: d) $[0, 1]$

83. A closed subspace of a compact metric space is -----Ans: compact.

84. If A and B are two compact subsets of a metric space M. Then $A \cup B$ is ----
Ans: compact.

85. Write Heine Borel theorem

Ans: Any closed interval $[a, b]$ is a compact subset of \mathbb{R} .

86. A subset A of \mathbb{R} is compact iff ----- Ans: A is closed and bounded.

87. Let A be a subset of metric space M .If A is totally bounded then A is ----
Ans: bounded.

88. Let A be totally bounded subset of \mathbb{R} . Then A is -----Ans: compact.

89. Continuous image of a compact metric space is ----- Ans : compact.

90. Any infinite subset of a compact metric space has a -----

Ans: Limit point

91. Any continuous function defined on a compact metric space is -----

Ans: uniformly continuous.

92. Any closed and bounded subset of \mathbb{R} is -----Ans: compact.

Say True or False

93. Any compact metric space is complete . Ans: True

94. Any totally bounded metric space is compact. Ans: False

95. Any closed and bounded subset of a metric space is compact. Ans: False

96. Any totally bounded and complete metric space is compact. Ans: True


97. A bounded infinite subset of \mathbb{R} has a limit point. Ans: True

98. Any totally bounded metric space is separable. Ans: True

99. Any compact metric space is separable. Ans: True

100. Any continuous real valued function defined on $[a, b]$ is bounded.

Ans: True


Staff in charge